

Relationship Specificity, Market Thickness and International Trade

— Keio University —

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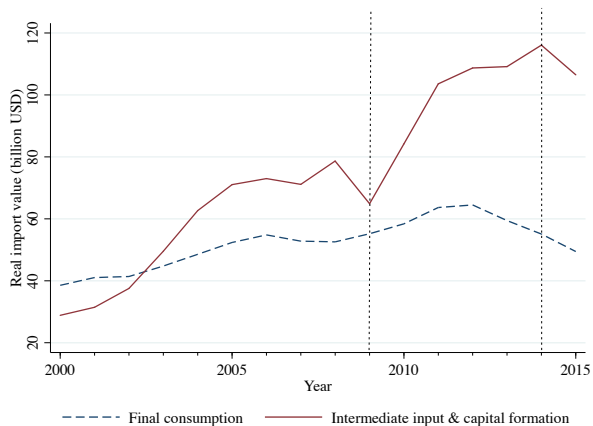
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Motivation

- Intermediate inputs have a large and growing share of international trade relative to final goods:
 - “Offshoring”
 - “Outsourcing”
 - “Vertical specialization”
 - “Fragmentation of production processes”

- Issues to be addressed:
 - Vertical linkages between upstream and downstream sectors
 - Welfare gains from trade associated with vertical linkages

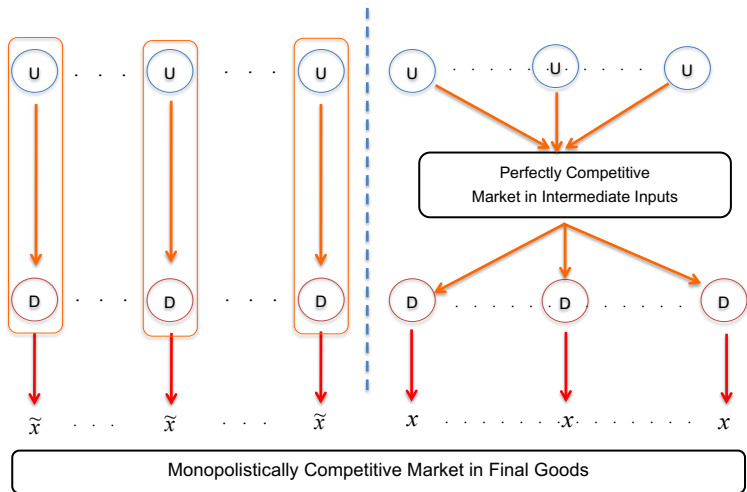
Motivation (cont.)



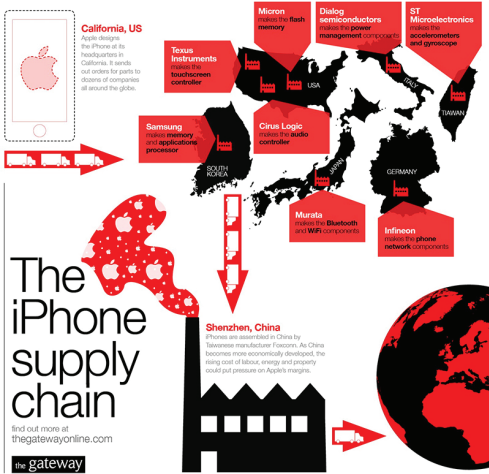
Japan's imports from China in 2000–2015

Source: Ito (2018)

Two types of input transactions



Example: smartphones



Non-market transaction

Example: smartphones (cont.)

Online Marketplace

Trade Shows

Smart Sourcing

Other Services

global sources
Reliable exporters: find them and meet them

Products

Enter English keyword to search products

Path: All Categories >> Mobile Electronics >> Mobile Phone Accessories & Parts >> Mobile Phone Parts >> Mobile phone LCDs -  Update me on new products



Smartphone parts LCD screen module for Moto E3

US\$ 9.5 / Piece

[Get Freight Cost](#)

50 Pieces Minimum Order


1 - 3 days Lead Time

Small Orders:

Accepted

Sample Price (USD):

\$15.00 [Request Sample](#)

 [Inquire Now](#)

 [Request Latest Price](#)

 [Add to Basket](#)

Market transaction (reference priced)

Market thickness

- Three ways for input procurement (Rauch, 1999; Nunn, 2007):
 - Sold on an organized exchange
 - Reference priced
 - Neither

Input customization measure

Sector	Proportion of inputs procured by "neither"
Automobile & light truck manuf.	0.980
Heavy duty truck manuf.	0.977
Electronic computer manuf.	0.956
...	...
Petroleum refineries	0.036
Flour milling	0.024
Poultry processing	0.024

Source: Nunn (2007)

Welfare gains from trade

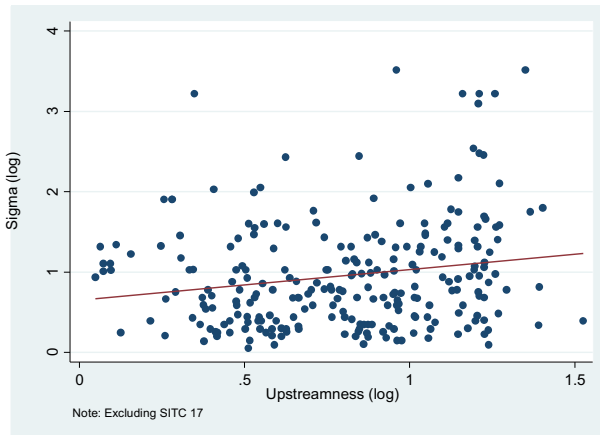
■ Sources of welfare gains:

- Resource reallocations from unmatched firms to matched firms
- Market restructure in vertical linkages

■ Empirically testable prediction:

- Trade liberalization increases the proportion of inputs procured by non-market transactions

Is the input market more competitive?



Note: Upstreamness from Antràs et al. (2012)

Elasticity of substitution from Broda and Weinstein (2006)

Outline

- Baseline model
- Closed-economy equilibrium:
 - Cross-industry variations between two transactions
- Open-economy equilibrium:
 - Welfare gains from improvement in matching environments
 - Country asymmetry in size
- Summary

Model

- Preferences:

$$U = \prod_{j=1}^J X_j^{\delta_j}, \quad \sum_j \delta_j = 1, \quad \delta_j > 0$$

where

$$X_j = \left[\int_{\omega \in \Omega_j} \alpha_j(\omega)^{\frac{1}{\sigma_j}} x_j(\omega)^{\frac{\sigma_j-1}{\sigma_j}} d\omega \right]^{\frac{\sigma_j}{\sigma_j-1}}, \quad \sigma_j > 1$$

- Demand in industry j :

$$x_j(\omega) = E_j P_j^{\sigma_j-1} \alpha_j(\omega) p_j(\omega)^{-\sigma_j}$$

Model (cont.)

■ Production:

	Unmatched	Matched
Input type	Generic	Customized
Input quality	$\alpha = 1$	$\alpha \in [\alpha_{\min}, \infty)$
Input transaction	Competitive market	Within pairs
U 's profit	$\pi^U = 0$	$\pi^U(\alpha)$
D 's profit	π^D	$\pi^D(\alpha)$
Joint profit	$\pi = \pi^D$	$\pi(\alpha) = \pi^D(\alpha) + \pi^U(\alpha)$

- α is randomly drawn from $G(\alpha) = 1 - \left(\frac{\alpha_{\min}}{\alpha}\right)^\gamma$ where $\alpha_{\min} > 1$
- c is common between matched and unmatched firms

Model (cont.)

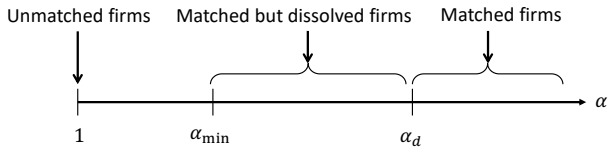
- Optimal profits:

$$\pi(\alpha) = \frac{E\alpha}{\sigma} \left(\frac{\frac{\sigma c}{\sigma-1}}{P} \right)^{1-\sigma}, \quad \pi = \frac{E}{\sigma} \left(\frac{\frac{\sigma c}{\sigma-1}}{P} \right)^{1-\sigma} \implies \frac{\pi(\alpha)}{\pi} = \alpha$$

- Cutoff quality:

$$\pi(\alpha_d) - k = \pi \implies \alpha_d = \frac{\pi + k}{\pi}$$

Model (cont.)



Sorting by product quality

Model (cont.)

- Average quality of matched firms:

$$\tilde{\alpha}_d = \int_{\alpha_d}^{\infty} \alpha \frac{dG(\alpha)}{1 - G(\alpha_d)} = \frac{\gamma}{\gamma - 1} \left(\frac{\pi + k}{\pi} \right)$$

- Average profit of matched firms:

$$\tilde{\pi} = \int_{\alpha_d}^{\infty} \pi(\alpha) \frac{dG(\alpha)}{1 - G(\alpha_d)} = \frac{\gamma}{\gamma - 1} (\pi + k)$$

Model (cont.)

■ Search technology $\nu(M - n, N - n)$:

- CRS in matching
- $\nu(\lambda a, \lambda b) = \lambda \nu(a, b)$

■ Probabilities of a match:

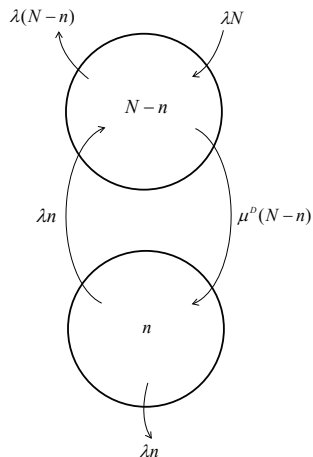
$$\check{\mu}^D = \frac{\nu(M - n, N - n)}{N - n} = \nu\left(\frac{M - n}{N - n}, 1\right) \equiv s(z)$$

$$\check{\mu}^U = \frac{\nu(M - n, N - n)}{M - n} = \nu\left(1, \frac{N - n}{M - n}\right) = \frac{s(z)}{z}$$

where $z \equiv (M - n)/(N - n)$

- $z \uparrow \Rightarrow \check{\mu}^D = s(z) \uparrow$
- $z \uparrow \Rightarrow \check{\mu}^U = s(z)/z \downarrow$

Model (cont.)



■ Search process (in steady state):

$$\begin{aligned} 2\lambda n &= \mu^U(M-n) \\ \underbrace{2\lambda n}_{\text{\# of breakdown pairs}} &= \underbrace{\mu^D(N-n)}_{\text{\# of newly matched pairs}} \end{aligned}$$

where

- λ : hazard rate of bankrupt
- $\mu^D \equiv [1 - G(\alpha_d)]\check{\mu}^D$
- $\mu^U \equiv [1 - G(\alpha_d)]\check{\mu}^U$

Closed-economy equilibrium

■ No-arbitrage conditions:

- Downstream firms

$$r\tilde{V}^D = \tilde{\pi}^D - \lambda(\tilde{V}^D - V^D) - \lambda\tilde{V}^D + \dot{\tilde{V}}^D$$

$$rV^D = \pi + \mu^D(\tilde{V}^D - V^D) - \lambda V^D + \dot{V}^D$$

- Upstream firms

$$r\tilde{V}^U = \tilde{\pi}^U - \lambda(\tilde{V}^U - V^U) - \lambda\tilde{V}^U + \dot{\tilde{V}}^U$$

$$rV^U = \mu^U(\tilde{V}^U - K - V^U) - \lambda V^U + \dot{V}^U$$

where K is a one-time relationship-specific investment

Closed-economy equilibrium (cont.)

■ Assuming that $r = 0$ and setting $\dot{\tilde{V}}^D = \dot{V}^D = \dot{\tilde{V}}^U = \dot{V}^U = 0$:

- Downstream firms

$$\tilde{V}^D = \left(\frac{\lambda + \mu^D}{2\lambda + \mu^D} \right) \frac{\tilde{\pi}^D}{\lambda} + \left(\frac{\lambda}{2\lambda + \mu^D} \right) \frac{\pi}{\lambda}$$

$$V^D = \left(\frac{\mu^D}{2\lambda + \mu^D} \right) \frac{\tilde{\pi}^D}{\lambda} + \left(\frac{2\lambda}{2\lambda + \mu^D} \right) \frac{\pi}{\lambda}$$

- Upstream firms

$$\tilde{V}^U - K = \left(\frac{\lambda + \mu^U}{2\lambda + \mu^U} \right) \left(\frac{\tilde{\pi}^U}{\lambda} - 2K \right)$$

$$V^U = \left(\frac{\mu^U}{2\lambda + \mu^U} \right) \left(\frac{\tilde{\pi}^U}{\lambda} - 2K \right)$$

Closed-economy equilibrium (cont.)

- Bargaining in matched pairs:

$$\begin{aligned}(\tilde{\pi}^D, \tilde{\pi}^U) &= \arg \max_{\tilde{\pi}^{D'}, \tilde{\pi}^{U'}} \left(\tilde{V}^{D'} - V^D \right) \left(\tilde{V}^{U'} - K - V^U \right) \\ \text{s.t. } &\tilde{\pi}^{D'} + \tilde{\pi}^{U'} = \tilde{\pi}\end{aligned}$$

- FOCs:

$$\begin{aligned}\frac{\tilde{\pi}^D}{\lambda} - \frac{\pi}{\lambda} &= \beta \left(\frac{\tilde{\pi}}{\lambda} - \frac{\pi}{\lambda} - 2K \right) \\ \frac{\tilde{\pi}^U}{\lambda} - 2K &= (1 - \beta) \left(\frac{\tilde{\pi}}{\lambda} - \frac{\pi}{\lambda} - 2K \right)\end{aligned}$$

where $\beta \equiv \frac{\mu^D + 2\lambda}{\mu^D + \mu^U + 4\lambda}$

Closed-economy equilibrium (cont.)

- FE conditions:

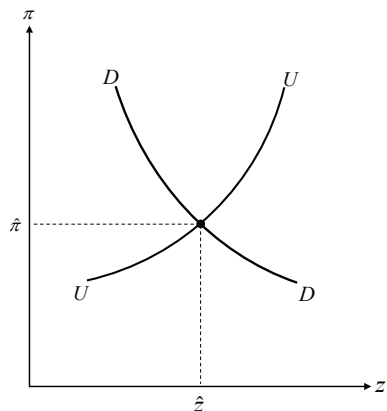
$$V^D = F^D, \quad V^U = F^U$$

which can be written as

$$\begin{aligned}\pi + \frac{n}{N}\beta(\tilde{\pi} - \pi - k) &= f^D \\ \frac{n}{M}(1 - \beta)(\tilde{\pi} - \pi - k) &= f^U\end{aligned}$$

where $f^D \equiv \lambda F^D$, $f^U \equiv \lambda F^U$, $k \equiv 2\lambda K$

Closed-economy equilibrium (cont.)

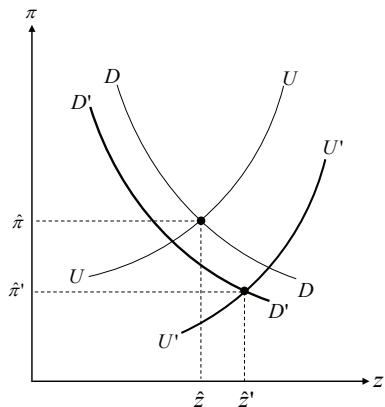


$$z = (M - n)/(N - n)$$

■ Unique equilibrium $\{\hat{z}, \hat{\pi}\}$:

- DD curve
 $z \uparrow \Rightarrow \mu^D = s(z) \uparrow \Rightarrow \pi \downarrow$
- UU curve
 $z \uparrow \Rightarrow \mu^U = s(z)/z \downarrow \Rightarrow \pi \uparrow$
- Other endogenous variables
($M, N, n, \alpha_d, \tilde{\alpha}_d, \tilde{\pi}$) can be written as a function of $\{\hat{z}, \hat{\pi}\}$

Closed-economy equilibrium (cont.)



■ Industries with $\gamma' < \gamma$:

$$\hat{z}' > \hat{z}, \hat{\pi}' < \hat{\pi}$$

■ Intuition:

- An industry with lower γ has a larger rent

$$\hat{\pi} - \pi - k = \frac{\pi + k}{\gamma - 1}$$

- From the FE conditions,

$$\hat{\pi} = f^D - f^U \hat{z}$$

Closed-economy equilibrium (cont.)

Proposition 1

The greater the dispersion of product quality (lower γ) of the industry, the smaller the market transaction

- The market thickness is given by

$$\frac{(N - n)p_x}{n\tilde{p}\tilde{x}} = \frac{2\lambda}{s(\hat{z})\tilde{\alpha}_d}$$

where

$$\gamma \downarrow \implies \begin{cases} \hat{z} \uparrow \\ \hat{\pi} \downarrow \end{cases} \implies \begin{cases} s(\hat{z}) \uparrow \\ \tilde{\alpha}_d \uparrow \end{cases}$$

Open-economy equilibrium

■ Suppose:

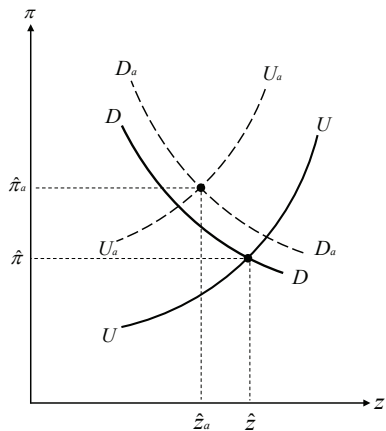
- Two symmetric countries start costly trade
- Trade costs allow only matched firms to export final goods
- Firms can search for partners from a foreign country and import inputs

■ FE conditions:

$$\pi + \frac{n}{N}\beta(\tilde{\pi} - \pi - k - \chi f_x) + \frac{n^*}{N}\beta(\tilde{\pi}^* - \pi - k - \chi^* f_x) = f^D$$
$$\frac{n}{M}(1 - \beta)(\tilde{\pi} - \pi - k - \chi f_x) + \frac{n^*}{M}(1 - \beta)(\tilde{\pi}^* - \pi - k - \chi^* f_x) = f^U$$

where χ is a proportion of exporting firms

Open-economy equilibrium (cont.)



■ Intuition:

- Export/import opportunity contributes to greater rents to matched pairs

■ Impact of trade:

$$\begin{cases} \hat{z} > \hat{z}_a \\ \hat{\pi} < \hat{\pi}_a \end{cases}$$

Open-economy equilibrium (cont.)

Proposition 2

Social welfare is higher in the open economy than in the closed economy due to:

- *Profit reallocations from unmatched firms to matched firms*

$$\frac{\tilde{\pi}}{\pi} = \frac{\tilde{\pi}^*}{\pi} > \frac{\tilde{\pi}_a}{\pi_a}$$

- *Increase in average product quality*

$$\tilde{\alpha}_d > \tilde{\alpha}_{da}$$

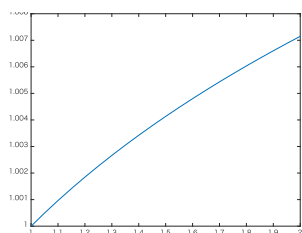
- *Increase in high-quality varieties*

$$s(\hat{z}) > s(\hat{z}_a)$$

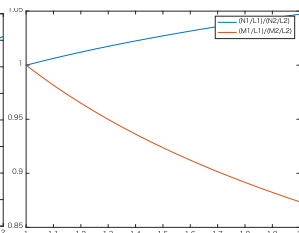
Country asymmetry: $L_1/L_2 \uparrow$

■ Impact of country size:

- Home market effect on wages and production patterns
- Agglomeration of final-good (intermediate-input) production in country 1 (country 2)

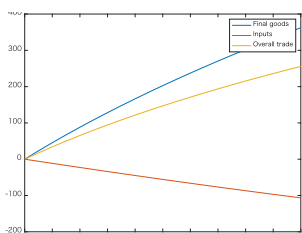


Relative wage (w_1/w_2)



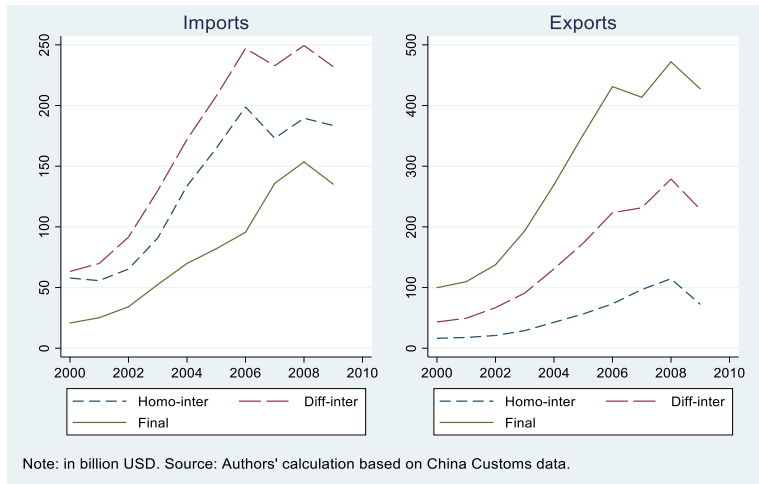
Ratio of firms (adjusted by size)

$$\frac{N_1}{N_2} > \frac{L_1}{L_2}, \quad \frac{M_1}{M_2} < \frac{L_1}{L_2}$$



Country 1's trade balance

Country asymmetry: $L_1/L_2 \uparrow$ (cont.)



China's trade in 2000-2009

Conclusion

■ Main findings:

- The higher the input customization, the greater non-market transactions
- Trade liberalization improves matching environments in vertical linkages

■ Future work:

- Multi-country model with some empirical evidence
- International agglomeration in vertical linkages